

Problem Mermaid of the Waters

Input file `stdin`
Output file `stdout`

*The title of the problem has as much to do
with the statement
as Denise's lyrics have to do with Marius's
(for those who know).*

On a 0-indexed binary string S of length N , you can apply the following operation any number of times:

- Choose an index i ($0 \leq i < N - 1$) such that $S_i = S_{i+1}$ and remove S_i and S_{i+1} from S .

After this operation, we get the string $S_0 \dots S_{i-1} S_{i+2} \dots S_{N-1}$

Given a positive integer N , Conte the Swedish asks you to find the number of binary strings of length N that can become empty after applying the operation above on them any number of times. Since this number can be very large, calculate it modulo $10^9 + 9$.

Input data

The only line of the input will contain the number N .

Output data

Output a single number, the number of binary strings of length N that can become empty after applying the operation any number of times.

Restrictions

- $1 \leq N \leq 2 \cdot 10^5$.

| # | Points | Restrictions |
|---|--------|--------------------------|
| 1 | 3 | $1 \leq N \leq 6$ |
| 2 | 11 | $1 \leq N \leq 16$ |
| 3 | 38 | $1 \leq N \leq 1\,000$ |
| 4 | 48 | No further restrictions. |

Examples

| Input file | Output file |
|------------|-------------|
| 4 | 6 |

Explanations

The 6 strings are 1111, 0000, 1100, 0011, 0110, 1001.