

## Find the Permutation (findperm)

 This is an interactive problem. Your program communicates with the evaluator: it should alternately write messages to the evaluator on the standard output and read the next input from the standard input.

There is a hidden permutation  $P = [P_1, P_2, \dots, P_N]$  of the numbers  $1, 2, \dots, N$ .<sup>1</sup>



Figure 1: The permutation, hidden between two walls.

You can ask questions in the form  $(i, j)$  with  $1 \leq i, j \leq N$ . Note that  $i$  and  $j$  does not have to be distinct.

The evaluator responds with the **most significant bit** of the bitwise AND of  $P_i$  and  $P_j$ .<sup>2</sup> Here, the most significant bit of a number  $x$  is the exponent of the highest power of 2 that appears when writing  $x$  in base 2. For example, the most significant bit of  $5 = 101_{(2)}$  is 2, since  $2^2$  appears in the binary representation of 5. If the bitwise AND of  $P_i$  and  $P_j$  is 0, the evaluator responds with  $-1$ .

Your task is to determine the hidden permutation of at most 1000 numbers by asking no more than 30 000 questions.

 Among the attachments of this task you may find a template file `findperm.*` with a sample incomplete implementation.

### Input

The first line of the input contains the number  $N$ , the length of the permutation. After reading  $N$ , you can ask questions by printing them to the standard output in the following format:

```
? i j
```

where  $i$  and  $j$  describe the question  $(i, j)$ .

<sup>1</sup>A permutation of the numbers  $1, 2, \dots, N$  is a sequence of length  $N$  consisting of the numbers  $1, 2, \dots, N$ , containing each number exactly once.

<sup>2</sup>The bitwise AND of two numbers  $x$  and  $y$  is the number that contains the common bits of  $x$  and  $y$ . For example, if  $x = 11 = 1011_{(2)}$  and  $y = 13 = 1101_{(2)}$ , then their bitwise AND will be  $9 = 1001_{(2)}$ .

For each question, if  $i$  and  $j$  are between 1 and  $N$  (inclusive) and the solution has not asked more than 30 000 questions, you receive the answer. Otherwise, you receive  $-100$  and the evaluator terminates the interaction immediately with an 'Output isn't correct' verdict.

Once found, you have to print the hidden permutation in the following format:

!  $P_1 P_2 \dots P_N$

Printing the hidden permutation is not counted as a question.

After guessing the hidden permutation, or receiving the  $-100$  answer from the evaluator, your program shall terminate immediately, otherwise you might receive a 'Time limit exceeded' verdict.

## Constraints

- $1 \leq N \leq 1000$ .

## Scoring

Your program will be tested against several test cases. The test cases are being scored **independently**, and your final score is the sum of the scores of the test cases. The evaluator is **not adaptive**, meaning that in each test case, the hidden permutation is fixed before your program asks any questions.

Let  $Q$  denote the number of questions asked by your program in a test case. Then, your score for this test case is calculated in the following way:

- If  $Q > 30\,000$  you will get 0% of the points for the test;
- If  $25\,000 < Q \leq 30\,000$  you will get 20% of the points for the test;
- If  $20\,000 < Q \leq 25\,000$  you will get 40% of the points for the test;
- If  $15\,000 < Q \leq 20\,000$  you will get 60% of the points for the test;
- If  $Q \leq 15\,000$  you will get 100% of the points for the test.

## Examples

input	output
5	? 1 5
2	? 2 3
1	? 4 3
-1	? 4 4
0	! 4 3 2 1 5

## Explanation

Suppose that the hidden permutation is  $P = [4, 3, 2, 1, 5]$ . The first question asks the most significant bit of the numbers  $P_1 = 4$  and  $P_5 = 5$ , which is 2.

The second one asks about the hidden numbers 3 and 2, for which the answer is 1.

The bitwise AND of numbers 2 and 1 is 0 and thus, the answer for the third question will be  $-1$ .

Lastly, the answer to the fourth question is 0, because the bitwise AND of 1 and 1 is 1.

Note that this is just a sample interaction to showcase the process of asking questions, receiving answers, and guessing the hidden permutation. It **does not** necessarily represent an approach to finding the hidden permutation.